## Variation of the constants in the early and late universe

Jean-Philippe Uzan

Laboratoire de Physique Théorique, Orsay

Institut d'Astrophysique de Paris

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Phi in the sky, Porto

## Outline

- Tests of gravity on astrophysical scales
- Update of constraints on variation of some constants G /  $\alpha$  /  $\mu$  mainly
- Variation of the constants in the late universe Links with quintessence Model building
- Variation of the constants in the early universe

# Tests of gravity on astrophysical scales

In the standard cosmological model:

1- gravitation is supposed to be described by general relativity

2- spacetime geometry is assumed to have FLRW symmetries It follows that most observations depend only on E(a)

$$H(a) = H_0 E(a)$$

$$E^{2}(z) = \Omega_{m}^{0}(1+z)^{3} + \Omega_{r}^{0}(1+z)^{4} + \Omega_{K}^{0}(1+z)^{2}$$

e.g. : luminosity distance, angular distance, growth factor of perturbations

If matter content of the universe = matter + radiation Combined data of SNIa, CMB, LSS



- 1- Not in agreement with (standard) matter content
  - 2- Universe is accelerating  $\Omega_{\Lambda}^{0} \sim 0.7$  ,  $\Omega_{m}^{0} \sim 0.3$

**Gravitation** = any long range force that cannot be screened

## Variety of scenarios



## What can/should we test?

Many tests from mm to Solar System size both on a possible fifth force and universality of free fall

(See Adelberger and Esposito-Farèse talks)

#### Very few tests on astrophysical scales

Cluster scale (2 Mpc): X-ray vs lensing.Allen et al. MNRAS 324 (2001) 877but: galaxy rotation curvesAguire et al. CQG 18 (2001) R223

#### No direct test on cosmological scales

entangle properties of matter and gravity acceleration of the universe

#### What to test:

field equations (Poisson equation in the Newtonian limit)

EEP: local Lorentz invariance local position invariance: universality of free fall

Jacobson et al., gr-qc/0404067

#### constants

## Growth of cosmic structures

In a flat FLRW with  $\Lambda$ =0, growth factor  $D_+ \propto a_-$ 

In fact scaling depends on the equation of state and of the matter components.

In the weakly NL regime, the growing modes bring independent information on:

1- equation of state

Benabed and bernardeau, PRD 64 (2001) 083501

2- Poisson equation

Sealfon et al., astro-ph/0404111

3- various couplings of quintessence to e.g. dark matter Amendola and Quercellini, PRL 92 (2004) 181102; Reis et al., PRD69 (2004) 101301

## Test of the Poisson equation

On sub-Hubble scales, the gravitational potential and density contrast are related by



Toy model: 4D-5D gravity (brane induced)  $^{wavelength, k/(h^{-1}Mpc)}$ 

perturbations freeze on large scales (idem as effect of  $\Lambda)$  power spectra of  $\Phi$  and  $\delta$  are not identical

JPU and Bernardeau, Phys. Rev. D 64 (2001) 083004; White and Kochanek, ApJ 560 (2001) 539

## **Distance duality relation**

Photons travel on null geodesics Geodesic deviation equation holds Etherington, Phil. Mag. 15 (1933) 761; Ellis, 1971

**Reciprocity relation**: 
$$r_s = r_o(1+z)$$





## **Observational prospects**

Background observations ( $D_L$ ,  $D_A$ ,...) alone cannot allow to make the difference.

e.g. Reconstruction of ST theories requires H(z) and  $\delta(z)$ 

(Esposito-Farèse talk)

Weak lensing observation + SNIa data will allow to reconstruct H(z),  $\delta(z)$  and  $\Phi(z)$ .

in particular, one can apply the test of the Poisson equation

Variation of the constants is a test of Einstein equivalence principle on astrophysical scales Strong equivalence principle (G)

# Constraints on variation of some constants

Many tests concerning various constants  $\alpha$ ,  $\mu$ , G mainly.

Tests on different time scales:

local	(z=0)	atomic clocks, Solar System
geophysical	(z=0.10.4)	Oklo, meteorites
astrophysical	(z=0.2-3.5)	quasars
cosmological	(z=10 <sup>3</sup> , 10 <sup>8</sup> )	CMB, BBN.

I consider only dimensionless constants

Okun, Sov. Phys. Usp. 34 (1991) 818, Ellis and JPU, Am. J. Phys. (2004)

General reviews: JPU, RMP 75 (2003) 425; Ann. H. Poincaré 4 (2003) 347; Damour, gr-qc/0210059; gr-qc/0306023; Martins, astro-ph/0405630.





## Fine structure constant : laboratory

Based the comparison of atomic clocks using different transitions and atoms:



4 years, assume  $g_p$  constant

 $\dot{lpha}/lpha = (- \ 0.4 \pm 16) imes 10^{-16} \, {
m yr}^{-1}$  Marion et al., PRL 90 (2003) 150801

#### Comparison of <sup>199</sup>Hg+ and <sup>133</sup>Cs

3 years, in fact constraint on  $g_{cs}\mu\alpha^{0.6}$ 

 $|\dot{\alpha}/\alpha| < 1.2 \times 10^{-15} \, \mathrm{yr}^{-1}$ 

Bize et al., PRL 90 (2003) 150802

## Fine structure constant : laboratory

#### Comparison of H (1s-2s) and <sup>133</sup>CS

4 years combined with data on Rb gives Fischer et al., physics/0312086

$$\dot{\alpha}/\alpha = (-0.4 \pm 16) \times 10^{-16} \,\mathrm{yr}^{-1}$$
  
 $\mathrm{d} \ln(\mu_{cs}/\mu_{rb})/\mathrm{d}t = (-0.5 \pm 1.7) \times 10^{-15} \,\mathrm{yr}^{-1}$ 

#### Comparison <sup>171</sup>Yb+ and <sup>133</sup>Cs

 $\dot{lpha}/lpha=(-\,0.3\pm2.0) imes10^{-15}\,\mathrm{yr}^{-1}$  Peik et al., physics/0402132

Local constraints

What is measured: relative drift of the frequencies of two transitions Give constraints on combination of various constants Modelisation of  $F_{rel}$  / dependence of magnetic moments

Necessity to use various atoms

Karshenboim, physics/0311080

## Fine structure constant : Oklo

Natural nuclear reactor in Gabon, operating 1.8 Gyr ago (**z~0.14**) Shlyakhter, Nature **264** (1976) 340 Damour, Dyson, NPB **480** (1996) 37 Fujii et al., NPB **573** (2000) 377 Lamoreaux, torgerson, nucl-th/0309048 Flambaum, shuryak, PRD**67** (2002) 083507

Abundance of Samarium isotopes  $^{149}\text{Sm} + n \rightarrow ^{150}\text{Sm} + \gamma \qquad E_r = 0.0973 \,\text{eV}$ 

From isotopic abundances of Sm, U and Gd, one can measure the cross section averaged on the thermal neutron flux

$$\hat{\sigma}_{149}(T, E_r) = 91 \pm 6 \,\mathrm{kb}$$

From a model of Sm nuclei, one can infer  $s = \Delta E_r / \Delta \ln \alpha$ 

s~1Mev so that  $\Delta \alpha / \alpha \sim 1 Mev / 0.1 eV \sim 10^{-7}$ 

 $\Delta lpha / lpha = (0.5 \pm 1.05) imes 10^{-7}$  Damour, Dyson, NPB **480** (1996) 37

Fujii et al., NPB **573** (2000) 377 **2 branches.** 

## Fine structure constant : meteorites

Bounds on the variation of couplings can be obtained by Constraints on the lifetime of long-lives nuclei ( $\alpha$  and  $\beta$  decayers)

For 
$$eta$$
 decayers,  $\lambda \sim \Lambda (\Delta E)^p \propto G_F^2 lpha^s$ 

**Rhenium:**  $^{187}_{75} \text{Re} \longrightarrow ^{187}_{76} \text{Os} + \bar{\nu}_e + e^-$  Peebles, Dicke, PR 128 (1962) 2006  $\Delta E \sim 2.5 \text{ keV}, \quad s \sim -18000$ 

Use of laboratory data +meteorites data

$$-24\times 10^{-7} < \Delta\alpha/\alpha < 8\times 10^{-7}$$

Olive et al., PRD 69 (2004) 027701

Caveats: meteorites datation / averaged value

## Fine structure constant : CMB

It changes the recombination history 1- modifies the optical depth 2- induces a change in the hydrogen and helium abundances (x<sub>e</sub>)

$$\dot{\tau} = x_e n_e c \sigma_T$$

Effect on the position of the Doppler peak on polarization (reionisation)

Degeneracies:

cosmological parameters

electron mass  $\sigma_T \propto lpha^2/m_e$ 

origin of primordial fluctuations

**Analysis of WMAP data** 

$$\Delta \alpha / \alpha = (-1.5 \pm 3.5) \times 10^{-2} \qquad z \sim 10^3$$

Martins et al. PLB 585 (2004) 29; G. Rocha et al, N. Astron. Rev. 47 (2003) 863; see G. Rocha talk

## Fine structure constant : BBN

Big bang theory predicts abundances of D, <sup>3</sup>He, <sup>4</sup>He, <sup>7</sup>Li Mainly based on the balance between

- 1- expansion rate of the universe
- 2- weak interaction rate which controls n/p at the onset of BBN

Helium abundance

Campbell and Olive (1995); Kolb et al. (1986)

$$Y = \frac{2(n/p)_N}{1 + (n/p)_N} \qquad (n/p)_f \sim e^{-Q/kT_f} \qquad Q = a\alpha \Lambda_{QCD} + bv$$

Depends mainly on Q, T\_f and  $\tau_{\rm n}$   $G_F^2(kT_f)^5 = \sqrt{GN}(kT_f)^2$ 

Dependence of the nuclear rates on  $\boldsymbol{\alpha}$ 

Bergström et al (1999); Ichikawa and Kawasaki (2002)

Effects of 6 parameters: G,  $\alpha$ , v, m<sub>e</sub>, m<sub>q</sub>, Q

$$\Delta \alpha / \alpha = (6 \pm 4) \times 10^{-4} \qquad z \sim 10^{10}$$

Müller et al, astro-ph/0405373

## **Quasar observations**



## What news from the quasars



#### Alkali doublet

Si IV, 21 systems

 $\Delta \alpha / \alpha = (-0.5 \pm 1.3) \times 10^{-5}$ 

Murphy et al. MNRAS 327 (2003) 1237

2 < z < 3

To vary or not to vary, that is the question

Recent observations with VLT/UVES.

Chand et al., astro-ph/0401094 Srianand et al., astro-ph/0402177

MM have not been able to duplicate the previous results

Mg and Fe lines in a set of 23 systems

#### Systems selected with care

(prevent as much as possible from systematics instead of looking for them)

- \* only species with similar ionisation potential (MGII, FeII, SiII, AI II) (most likely to originate from similar regions in the cloud)
- \* reject absorption lines contaminated by atmospheric lines
- \* keep only FeII where multiplet detected at  $5\sigma$
- \* anchors (MgI an II) are not saturated.





## Much ado about nothing?



Analysis of a single quasar (z=1.15) Fe lines  $\Delta \alpha / \alpha = (-0.1 \pm 1.7) \times 10^{-6}$ 

Quast et al., astro-ph/0311280

## From quasars to stellar nucleosynthesis

Results of both teams are sensitive to isotopic abundance of Mg.

Solar ratio are assumed <sup>24</sup>Mg:<sup>25</sup>Mg:<sup>26</sup>Mg=79:10:11

If one assumes pure <sup>24</sup>Mg then

$$\Delta \alpha / \alpha = (-0.98 \pm 0.13) \times 10^{-5}$$
 Keck/Hires  
$$\Delta \alpha / \alpha = (-0.36 \pm 0.06) \times 10^{-5}$$
 VLT/UVES

It was proposed that apparent variation of  $\alpha$  can be explained by early nucleosynthesis <sup>8.6</sup> of <sup>25,26</sup>Mg.

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Ashenfelter et al., PRL92 (2004) 041102
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Hypothesis can be tested by correlations among other heavy elements.

First explanation that does not involve new physics.



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## New tests: OIII emission lines

OIII emission lines of distant quasars or galaxies

$$\Delta\lambda/\lambda\proptolpha^2$$

## Application on SDSS EDR

(42 quasars between z=0.16 to 0.80)

$$\Delta \alpha / \alpha = (0.7 \pm 1.4) \times 10^{-4}$$

Analysis of SDSS DR1 (165 quasars)

$$\Delta \alpha / \alpha = (1.2 \pm 0.7) \times 10^{-4}$$





Bahcall et al., ApJ 600 (2004) 520.

## New tests: OH microwave transitions

The 18cm OH line is both a hyperfine transition and a transition between lambda-doublet levels .

The transitions can be shown to behave as

$$\nu_{3/2} = \Lambda \alpha^{0.4} \pm (\Delta^+ \pm \Delta^-) \alpha^4$$



Darling, PRL 91 (2003) 011301

Preliminary application to quasar PKS 1413+135

$$\Delta \alpha / \alpha = (0.51 \pm 1.26) \times 10^{-5}, \qquad z = 0.2467$$

Darling, astro-ph/0405240

Method can be extended to z~5 Can improve sensitivity by correlating with CO lines

## **Gravitational constant**

Few improvements in the past years

Constancy of G: test of the strong equivalence principle e.g. ST theories have EEP but not SEP

Solar System experiment LLR:  $\dot{G}/G = (0 \pm 6) \times 10^{-12} \,\mathrm{yr}^{-1}$  Dickey et al. (1994)

PPN can give a bound but in a theoretical frame

Stellar constraints

 white dwarfs:
  $\dot{G}/G = (2 \pm 2) \times 10^{-11} \,\mathrm{yr}^{-1}$  Garcia-Berro et al. (1998)

 heliosysmology:
  $\dot{G}/G = (0 \pm 1.6) \times 10^{-12} \,\mathrm{yr}^{-1}$  Garcia-Berro et al. (1998)

BBN: roughtly 20%

## **Other studies**

Effects of other constants have started to be investigated e.g. Mass of quarks (BBN, Oklo...)



Ivanchik et al., Astrophys. Space Sci. 283 (2003) 583

In GUT and string inspired theories, gauge couplings are related at some unification scale



Calmet, Fritzsch, EPJ C24 (2002) 639; Dent, Fairbairn, NPB 653 (2003) 256

Allow to derive sharper bounds on variation of constants (BBN / Oklo)

## Summary



## Theory and phenomenology

Comparison of the compatibility of data can not be done in a model independent way.

Low energy limit of string theory: dilaton dimensionless constants depend on dilaton and volume of extra-dimensions.

Slow rolling field: quintessence field (?)

But some problems to be faced: 1- fields are light 2- UFF

Large number of studies.

## **Theoretical motivations**

In string theory, all dimensionless parameters become VEV of some fields: **dynamical**.

e.g. 
$$M_4^2 = e^{-2\Phi} V_6 M_I^8$$
  $g_{YM}^{-2} = e^{-\Phi} V_6 M_I^6$   $(+ c_i M_i)$   
 $G \propto R^{-D},$   $g_{YM}^{-2} \propto K_i(D) G R^2$ 

The low energy limit are scalar-tensor theories (dilaton) at tree level.

Loop corrections: need to be understood better couplings are not universal Dudas (2000)

$$M_4^2 = \phi M_H^8, \qquad g_{YM}^{-2} = \phi M_H^6, \qquad \phi = V_6 e^{-2\Phi}$$
$$g_{YM}^{-2} = \phi M_H^6 - \frac{b_a}{2} (RM_H^2) + \dots$$

Phenomenologically: couplings of the quintessence field brane models Palma et al PRD 68 (2003) 123519.

## Phenomenology: general frameworks

Bekenstein model:  $e = e_0 \varepsilon(x^{\mu})$ 

reduces to a coupling of a scalar field to electromagnetism

Bekenstein (1982) Olive, Pospelov (2002) Sandvik et al (2002) Avelino et al. (20004) Lee et al. (2004)

#### **String inspired models**

$$S = \int \mathrm{d}^4 x \sqrt{-g} \left( B_g(\phi) R - B_\phi(\phi) (\partial \phi)^2 - \frac{1}{4} B_F(\phi) F^2 - V(\phi) - \sum_a m_a(\phi) \sqrt{-g_{\mu\nu}} \, \mathrm{d}x^\mu \mathrm{d}x^\nu \right)$$

$$B_i(\phi) = e^{-\phi} + c_i^0 + c_i^1 e^{\phi} + \dots$$

Damour, Polyakov (1994)

A light scalar field satisfies a Klein-Gordon equation of the type  $\dot{\vec{\phi}}+3H\dot{\phi}=-m^2\phi+\ldots$ 

For the field to be slow-rolling today, one needs  $m\sim H_0\sim 10^{-33}\,{\rm eV}$ 

How can is the mass protected (symmetry?)

SUSY broken around the TEV general problem of quintessence models

#### Various solutions:

pseudo-Goldstone boson

Carroll, PRL81 (1998) 3067.

shape moduli: in the case of ST-quintessence, the total volume is coupled to gravity while shape moduli play the role of quintessence field

Peloso, Poppitz, hep-ph/0307379

## Dangers with the universality of free fall

Universality of free fall is tested with great accuracy  $\eta_{12} \equiv rac{|\vec{a_1} - \vec{a_2}|}{|\vec{a_1} + \vec{a_2}|}$ 

If there is a coupling of the form  $B(\phi)F_{\mu\nu}F^{\mu\nu}$  then the electromagnetic self energy contributes to the mass and  $m_i(\phi)$ 

Predictions require to know this  $m(\phi)$  (model dependent)

We expect a violation of UFF of order  $\eta_{12} \simeq M_p f_{\text{ext}} \partial_{\phi} \left| \ln(m_1/m_2) \right|$ 

e.g. from Baessler constraint:

 $|\nabla \ln \alpha| < 10^{-33} \,\mathrm{cm}$ 

## Avoiding UFF problems

In the Damour-Polyakov model, there is a cosmological attractor mechanism

Damour, Polyakov (1994)

1- requires all the  $B_i(\phi)$  to have a common local maximum

$$B_i(\phi) \simeq \text{const.} - \frac{1}{2}\kappa(\phi - \phi_m)^2$$

2- Einstein frame mass of hadrons are proportional to

$$\Lambda_{
m QCD} \propto B_F^{-1/2}(\phi)~{
m e}^{~-8\pi^2 b_3^{-1} B_F(\phi)} \Lambda_s$$

3- All deviations from GR (PPN parameters, dln $\alpha$ /dt,  $\eta$ ) are proportional to  $\Delta \phi^2 = (\phi_0 - \phi_m)^2$ 

The light scalar field can couple to different charges, e.g. in the case of<br/>dilaton fifth forceB=N+Zbaryon numberD=N-Zneutron excess $E=Z(Z-1)B^{1/3}$ Coulomb energy

$$\eta_{12} = \kappa^2 \Delta \phi^2 \left( C_B \Delta B + C_D \Delta D + C_E \Delta E \right) / M$$

Another recent (possibly) interesting proposal are chameleon fields.



ST theory with runaway potential Implementation in braneworld,

See Brax talk

Universal coupling Generalisation to varying  $\alpha$ ?

#### **Gravitational constant**:

In the framework of quintessence, extended models were shown to exhibit the same attractor mechanism JPU, PRD **59** (1999) 123510; Chiba gr-qc/9904120; Amendola gr-qc/9908023; Riazuelo, JPU, PRD66 (2002) 023525

> WEP valid: no problem with UFF Reconstruction problem studied Polarski, Esposito-Farèse,

#### Fine structure constant:

1- investigation of Bekenstein like models

2- generalization of Damour-Polyakov model to runaway dilaton Damour et al , PRD (2003)

#### Dark matter:

Possibility of coupling  $\phi$  to DM / few tests Amendola Damour et al. PRL64 (1990) 123 During inflation:

all light fields developp super-Hubble correlations

Two aspects:

1- couplings during inflation can be modulated2- there may exist a spatial distribution of the constants after inflation

## Modulated fluctuations

In the case of hybrid-inflation, the couplings may depend on light moduli

$$V = \frac{\lambda(\chi)}{4} (\sigma^2 - v^2)^2 + \frac{g^2(\chi)}{2} \varphi^2 \sigma^2 + V(\varphi)$$

Spinodal instability at  $\varphi_c = \frac{\sqrt{\lambda}v}{g}$ 

If moduli fields are light then  $\varphi_c$  will fluctuate and inflation will not end at the same « time » everywhere.

Kofman astro-ph/0303614; Dvali et al, PRD 69 (2004) 023505

## **Observational imprint**: consistency relation of inflation is modified

Bernardeau, Kofman, JPU, astro-ph/0403315

Light field: superhubble correlation.

Expect a spatial distribution of the constant 1- amplitude is typically of order 10<sup>-5</sup> This may alter the analysis of quasars It may be correlated with density fluctuations

Mota, Barrow, MNRAS 349 (2004) 281

2- CMB: the recombination may be modulated by the local value of the fine structure constant

-modification of the temperature power spectrum -generate polarisation B modes -induce non-Gaussianity Sigurdson et al,PRD **68** (2003) 103509

## Conclusions

Tests of gravity will substantiate the physics of the dark sector go beyond pure scalar field interacting with gravity local predictibility hypothesis

Variation of constants may be golden plate observations for quintessence-like models.

But, still models have to satisfy sharp constraints concerning

1- smallness of the mass

2- UFF

From an observational point of view, quasar analysis and compatibility between the 2 groups will require a long work

Future tests: e.g. ACES,  $\mu$ SCOPE, STEP

Interpretation of cosmological data in non GR frame needs care

String issue: Why are the constants so constant?